

# A hierarchical Bayesian approach for estimation of photosynthetic parameters of C<sub>3</sub> plants

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## ABSTRACT

We describe a hierarchical Bayesian (HB) approach to fitting the Farquhar *et al.* model of photosynthesis to leaf gas exchange data. We illustrate the utility of this approach for estimating photosynthetic parameters using data from desert shrubs. Unique to the HB method is its ability to simultaneously estimate plant- and species-level parameters, adjust for peaked or non-peaked temperature dependence of parameters, explicitly estimate the 'critical' intracellular [CO<sub>2</sub>] marking the transition between ribulose 1,5-bisphosphate carboxylase/oxygenase (Rubisco) and ribulose-1,5-bisphosphate (RuBP) limitations, and use both light response and CO<sub>2</sub> response curve data to better inform parameter estimates. The model successfully predicted observed photosynthesis and yielded estimates of photosynthetic parameters and their uncertainty. The model with peaked temperature responses fit the data best, and inclusion of light response data improved estimates for day respiration ( $R_d$ ). Species differed in  $R_{d25}$  ( $R_d$  at 25 °C), maximum rate of electron transport ( $J_{max25}$ ), a Michaelis-Menten constant ( $K_{c25}$ ) and a temperature dependence parameter ( $\Delta S$ ). Such differences could potentially reflect differential physiological adaptations to environmental variation. Plants differed in  $R_{d25}$ ,  $J_{max25}$ , mesophyll conductance ( $g_{m25}$ ) and maximum rate of Rubisco carboxylation ( $V_{cmax25}$ ). These results suggest that plant- and species-level variation should be accounted for when applying the Farquhar *et al.* model in an inferential or predictive framework.

**Key-words:** *Artemisia tridentata*; *Dasyllirion leiophyllum*; *Larrea tridentata*; *Purshia tridentata*; A–C<sub>i</sub> curve; A–Q curve; Farquhar *et al.* model;  $J_{max}$ ; photosynthesis;  $V_{cmax}$ .

## INTRODUCTION

Mechanistic photosynthetic models based on phenomenological descriptions of the underlying biochemical reactions have broad applications in the field of plant ecophysiology. These models may be used to determine the impact

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of varying environmental conditions – including those predicted to be affected by climate change – on the biochemistry of photosynthesis and carbon acquisition at the leaf and plant levels (e.g. Wohlfahrt, Bahn & Cernusca 1999a). Further, mechanistic photosynthetic models are often used to parameterize vegetation components in process models applied at scales ranging from plant canopies (Baldochi & Harley 1995; dePury & Farquhar 1997) to landscapes (Kimball *et al.* 2000; Williams *et al.* 2001) to continents (Sellers *et al.* 1996; Foley *et al.* 1998; Pitman 2003). As such, photosynthetic parameters associated with leaf-level models provide valuable, mechanistic information for predicting large-scale effects of future climate change on terrestrial ecosystems.

In the most commonly used mechanistic model of C<sub>3</sub> photosynthesis, carbon assimilation is limited by one of three biochemical processes (Farquhar, von Caemmerer & Berry 1980). That is, the rate of photosynthesis is modelled as the minimum of three functions: (1) the saturation of ribulose 1,5-bisphosphate carboxylase/oxygenase (Rubisco) with respect to carboxylation; (2) electron transport limiting the regeneration of ribulose-1,5-bisphosphate (RuBP); and (3) the amount of triose phosphate exported from the chloroplast. Through fitting this 'Farquhar *et al.*' model (Farquhar *et al.* 1980) to photosynthetic gas exchange measurements (e.g. photosynthetic responses to changes in intercellular CO<sub>2</sub> concentrations; A–C<sub>i</sub> curve), the following parameters can be estimated: the maximum Rubisco carboxylation rate ( $V_{cmax}$ ), the maximum rate of electron transport ( $J_{max}$ ), mitochondrial respiration in the light ( $R_d$ ) and mesophyll conductance ( $g_m$ ). Because of the crucial role these parameters play in scaling photosynthesis, it is essential that accurate estimates of these parameters are obtained when fitting mechanistic photosynthetic models to leaf-level empirical data.

Importantly, estimates of the photosynthetic parameters of interest (e.g.  $V_{cmax}$ ,  $J_{max}$ ) are sensitive to the statistical estimation methods used to fit the Farquhar *et al.* model (Manter & Kerrigan 2004; Dubois *et al.* 2007; Miao *et al.* 2009). These fitting methods are not yet consistent in the literature and can be categorized into six distinct methods (see Miao *et al.* 2009 for a comprehensive review). The primary difference among these methods is the statistical approach used to determine the transition C<sub>i</sub> value ( $C_{crit}$ ; the

value of  $C_i$  used to differentiate between Rubisco and RuBP limitations). In addition to the statistical fitting approach, the accuracy of fitting the Farquhar *et al.* model also relies on: (1) correct representation of the kinetic properties of Rubisco (Sharkey *et al.* 2007), often assumed to be relatively conserved in  $C_3$  plants (von Caemmerer 2000); (2) incorporation of temperature dependencies of parameters, which are described by either exponential or peaked exponential functions (Leuning 1997, 2002; Wohlfahrt *et al.* 1999b; Medlyn, Loustau & Delzon 2002; Kattge & Knorr 2007); (3) incorporation of  $g_m$  (Niinemets *et al.* 2009a; Pons *et al.* 2009); and (4) accounting for species- and plant-level differences in both fixed parameters (e.g. kinetic constants), estimated parameters (e.g.  $V_{cmax}$ ,  $J_{max}$ ) and temperature dependencies.

Indeed, empirical studies have shown that model parameters do vary by plant and species as a result of genetic or environmental variation. For example, mesophyll conductance ( $g_m$ ), which partially controls the transfer of  $CO_2$  from the mesophyll intercellular space to the site of carboxylation, has been shown to respond to light and leaf anatomy (Evans & von Caemmerer 1996; Tholen *et al.* 2008; Warren 2008; Loreto, Tsonev & Centritto 2009). This variability is important to recognize, because variation in  $g_m$  has been linked to changes in photosynthetic capacity (von Caemmerer & Evans 1991; Lloyd *et al.* 1992; Loreto *et al.* 1992; Niinemets *et al.* 2009b). Rubisco kinetic constants (e.g.  $K_c$ ,  $K_o$ ) also change across diverse species and environmental conditions (Tcherkez, Farquhar & Andrews 2006). Paradoxically, while variability in such model parameters has been widely documented, many studies have not yet incorporated intra- and interspecific parameter variability into procedures for fitting the Farquhar *et al.* model. Subsequently, application of this model may incorrectly conclude that significant differences exist in parameter estimates for plants, species or treatments, thereby limiting the accuracy of this popular photosynthetic model.

In light of the need for accurate plant- and species-level estimates of photosynthetic parameters under varying environmental conditions, we describe a statistically rigorous method to estimate  $C_3$  photosynthetic parameters. Specifically, we implemented a hierarchical Bayesian (HB) framework that couples the Farquhar *et al.* model with multiple photosynthetic data sets, allowing estimation of plant- and/or species-level variability of kinetic constants and biochemical parameters. While other gas exchange data (e.g.  $A-Q$ ; light response curves) are often collected in conjunction with  $A-C_i$  curves, these data are rarely incorporated into the fitting procedure, although they may help to inform the biochemical processes regulating photosynthesis (von Caemmerer 2000). Here, we use both  $A-C_i$  and  $A-Q$  data to simultaneously estimate all photosynthetic parameters, including a  $C_{crit}$  value specific to each curve. Another attractive feature of the HB approach is that we can explicitly accommodate the nested sampling design such that the photosynthetic parameters are modelled hierarchically (e.g. curves/plants nested in species).

To illustrate and evaluate the HB approach, we used field data collected from four species of common North American desert shrubs. Desert plants were chosen because their photosynthetic responses differ greatly from temperate forest and agricultural species – which are most commonly studied with respect to parameterizing the Farquhar *et al.* photosynthetic model – based on sensitivity to water limitation and temperature (Ogle & Reynolds 2002). By comparing HB model parameter estimates for desert plants with estimates in the literature from temperate forest and crop plants, we highlight the potential importance of incorporating: (1) flexibility in defining kinetic and biochemical parameter values; (2) plant- and species-specific parameter variability when estimating photosynthetic parameters; and (3) more rigorous statistical methods for analyzing photosynthetic data in the context of mechanistic models such as the Farquhar *et al.* model.

## METHODS

### Study sites, plants and field measurements

Photosynthetic data for shrub species used in this study were collected at three study sites, each within a distinct North American desert ecosystem. In the Great Basin Desert, the field site was located near the Sierra Nevada Aquatic Research Laboratory (SNARL) of the Valentine Eastern Sierra UC (University of California) Natural Reserve, in eastern California near the city of Mammoth Lakes (37°37'N, 118°50'W, elevation 2100 m). Mean annual precipitation (MAP) is approximately 386 mm, most of which is received between October and March as snow or convective rainstorms. For more detailed SNARL site characteristics, see Gillespie & Loik (2004) and Loik (2007). In the Mojave Desert, data were collected at the Mojave Global Change Facility (MGCF) located on the Nevada Test Site (36°49'N, 115°55'W, elevation 970 m). MAP at the MGCF is about 138 mm, occurring primarily during the winter months (Hunter 1995), with highly episodic summer precipitation and a low relative frequency of large rainfall events. For a more detailed MGCF site description, see Barker *et al.* (2006). In the Chihuahuan Desert, the study site was located in a sotol grassland ecosystem within the Pine Canyon Watershed in Big Bend National Park (BIBE), Texas (29°5'N, 103°10'W, elevation 1526 m). MAP is about 370 mm, with the majority of annual precipitation occurring during the summer months and arriving as monsoonal rains. For a more detailed BIBE site description, see Patrick *et al.* (2007, 2009) and Robertson *et al.* (2009).

At SNARL, measurements were collected on *Artemisia tridentata* (ARTR; Asteraceae,  $n = 5$  plants) and *Purshia tridentata* (PUTR; Rosaceae,  $n = 5$  plants), two native  $C_3$  woody shrubs in the sagebrush scrub ecosystem. These species are codominant in the ecosystem, representing about 80% of the plant cover (Loik 2007). At MGCF, measurements were made on the native, dominant  $C_3$  evergreen shrub, *Larrea tridentata* (LATR; Zygophyllaceae,  $n = 4$  plants). At BIBE, measurements were made on the

dominant  $C_3$  perennial shrub, *Dasyliirion leiophyllum* (DALE; Liliaceae,  $n = 3$  plants).

During the 2005 growing season (May–August),  $A-Q$  curves (Supporting Information Fig. S1) were measured on each study plant at each site using a portable photosynthetic system (model Li-6400; Li-Cor, Lincoln, NE, USA). During the 2006 growing season (May–August), both  $A-C_i$  and  $A-Q$  curves were measured on the same study plants as the previous year.  $A-C_i$  curves were measured at saturating irradiance ( $1500 \mu\text{mol m}^{-2} \text{s}^{-1}$ ) for 12  $\text{CO}_2$  concentrations in the following order (first to last measurement): 0, 50, 100, 150, 200, 250, 380, 500, 700, 900, 1200 and  $1500 \mu\text{mol mol}^{-1}$ . To ensure steady-state conditions, the plants were allowed to acclimate to ambient  $\text{CO}_2$  ( $380 \mu\text{mol mol}^{-1}$ ) in the gas exchange chamber for approximately 5 min before beginning each  $A-C_i$  curve, and then logged. This logged measurement was then compared to the measurement at identical  $[\text{CO}_2]$  in the middle of the curve sequence to confirm full enzyme activation. It took approximately 45 min to complete a single  $A-C_i$  curve.  $A-Q$  curves were measured at ambient  $[\text{CO}_2]$  ( $400 \mu\text{mol mol}^{-1}$ ) for 12 light levels in the following order (first to last): 2000, 1500, 1000, 800, 600, 400, 300, 200, 100, 70, 40 and  $0 \mu\text{mol m}^{-2} \text{s}^{-1}$ . The plants were allowed to acclimate to changes in light intensity for approximately 2–3 min before measurements were logged; it took about 35 min to complete an entire  $A-Q$  curve.

Across all plants and curve types, leaf temperature and relative humidity were recorded and set to ambient values. Average temperature and relative humidity were  $26.1^\circ\text{C}$  and 48.9%, respectively, and ranged from  $11.2$  to  $44.4^\circ\text{C}$ , and from 7.2 to 94.1%, respectively. All curves were measured from the early morning to the early afternoon when day-time air temperature was near its daily minimum, vapour pressure deficit was relatively low and stomata were responsive to changes in  $\text{CO}_2$  and light. All measurements of photosynthesis and stomatal conductance were corrected for leaf area. A total of 17  $A-C_i$  curves and 37  $A-Q$  curves were measured across all species, providing 696 observations of photosynthesis.

## HB model of photosynthesis

Plant photosynthetic data were analysed within an HB framework (Clark 2005; Clark & Gelfand 2006). This approach has been successfully used to synthesize ecological data (e.g. Clark & LaDeau 2006; Ogle & Barber 2008), and it has proven to be exceptionally useful for making inferences about ecosystem and plant physiological responses (Cable *et al.* 2008, 2009; Ogle *et al.* 2009; Patrick *et al.* 2009). We propose that the HB approach is advantageous for modelling photosynthesis because it can: (1) simultaneously estimate unknown parameters – related to biochemical limitations of photosynthesis – while also accounting for uncertainty in measurements and parameters (Carlin, Clark & Gelfand 2006; Ogle & Barber 2008); (2) accurately estimate common photosynthetic parameters without the need for subjective determination of thresholds

for limiting biochemical processes [e.g. it allows us to avoid setting a fixed and potentially arbitrary transition intracellular  $\text{CO}_2$  ( $C_{\text{crit}}$ ) value to separately estimate  $V_{\text{cmax}}$  and  $J_{\text{max}}$ ]; (3) simultaneously incorporate a variety of data types (e.g.  $A-C_i$  and  $A-Q$  curve data) to arrive at parameter estimates and parameter variability; (4) allow for borrowing of strength between curves to help estimate population-level parameters of interest (e.g. species-specific biochemical parameters); and (5) incorporate prior information for biochemical parameters that may not be well informed by the  $A-C_i$  and  $A-Q$  response curve data, but that reflect appropriate levels of uncertainty based on variation in these parameters as reported in the literature. We emphasize that the HB model provides the statistical framework for fitting a process-based model such as the Farquhar *et al.* model to observational data. That is, we do not present modifications to the Farquhar *et al.* model, but describe a rigorous and statistically consistent methodology for confronting such a model with diverse data.

The HB model has three primary components: (1) the observation equation that describes the likelihood of observed photosynthesis data; (2) the process equation that describes the ‘true’ or mean photosynthetic response, based on the Farquhar *et al.* model of  $C_3$  photosynthesis, as well as process uncertainty associated with random effects; and (3) prior distributions for process model parameters (e.g. species effects) and variance terms. These three parts are combined to generate posterior distributions of all unknown parameters (see Wikle 2003; Clark 2005), including photosynthesis-related parameters and all variance/covariance terms. All probability distributions are parameterized according to Gelman *et al.* (2004). Table 1 includes a list of abbreviations and units for parameters used in the model. The model was run with two different photosynthetic data sets: (1) observations for  $A-C_i$  curves only ( $n = 207$ ); and (2) observations from both  $A-Q$  and  $A-C_i$  curves ( $n = 696$ ) to determine if  $A-Q$  curve data can improve estimates of photosynthetic parameters.

## The observation equation

The likelihood of all leaf-level photosynthesis data is based on the likelihood of individual observations of photosynthesis obtained from the Li-6400 (i.e.  $A_{\text{obs}}$ ;  $\mu\text{mol m}^{-2} \text{s}^{-1}$ ). We assumed that the photosynthetic measurements could be described by a normal distribution, such that for observation  $i$  ( $i = 1, 2, \dots, N$ ):

$$A_{\text{obs}_i} \sim \text{Normal}(\bar{A}_i, \tau) \quad (1)$$

where  $\bar{A}_i$  is the mean or predicted photosynthesis rate, and  $\tau$  is the precision (1/variance) parameter that describes the variability in the photosynthetic observation or measurement errors.

## The process model

The process model describes the predicted photosynthesis rate ( $\bar{A}_i$ ), which was specified according to the Farquhar

**Table 1.** List of abbreviations used in the coupled hierarchical Bayesian (HB)–photosynthetic model, their definitions and units

Abbreviation	Definition	Units
Observed data for model input		
<i>Aobs</i>	Rate of CO <sub>2</sub> assimilation measured by the Li-Cor 6400	μmol m <sup>-2</sup> s <sup>-1</sup>
<i>Ciobs</i>	Intercellular airspace CO <sub>2</sub> partial pressure measured by the Li-Cor 6400	Pa
<i>Qobs</i>	Photosynthetically active radiation measured by the Li-Cor 6400	μmol m <sup>-2</sup> s <sup>-1</sup>
<i>Tobs</i>	Leaf temperature measured by the Li-Cor 6400	°C
<i>Pobs</i>	Pressure measured by the Li-Cor 6400	Pa
HB model parameters associated with process model		
$\bar{A}$	Predicted rate of CO <sub>2</sub> assimilation (see Eqn 1)	μmol m <sup>-2</sup> s <sup>-1</sup>
<i>A<sub>c</sub></i>	Rubisco-limited rate of CO <sub>2</sub> assimilation	μmol m <sup>-2</sup> s <sup>-1</sup>
<i>A<sub>j</sub></i>	Electron transport limited rate of CO <sub>2</sub> assimilation	μmol m <sup>-2</sup> s <sup>-1</sup>
<i>E</i> ( <i>E<sub>g</sub></i> , <i>E<sub>m</sub></i> , <i>E<sub>r</sub></i> , <i>E<sub>kc</sub></i> , <i>E<sub>ko</sub></i> , <i>E<sub>v</sub></i> , <i>E<sub>j</sub></i> )	Activation energy used in Arrhenius temperature function	kJ mol <sup>-1</sup>
<i>f</i>	Spectral light quality factor	
<i>g<sub>m</sub></i>	Conductance for CO <sub>2</sub> diffusion from intercellular airspace to site of carboxylation	μmol m <sup>-2</sup> s <sup>-1</sup> Pa <sup>-1</sup>
<i>H</i> ( <i>H<sub>gm</sub></i> , <i>H<sub>v</sub></i> , <i>H<sub>j</sub></i> )	Deactivation factor used in Arrhenius temperature function	kJ mol <sup>-1</sup>
<i>J</i>	Rate of electron transport	μmol m <sup>-2</sup> s <sup>-1</sup>
<i>J<sub>max</sub></i> ( <i>J<sub>max25</sub></i> )	Maximal electron transport rate (standardized to 25 °C)	μmol m <sup>-2</sup> s <sup>-1</sup>
<i>K<sub>c</sub></i> ( <i>K<sub>c25</sub></i> )	Michaelis–Menten constant for Rubisco for CO <sub>2</sub> (standardized to 25 °C)	Pa
<i>K<sub>o</sub></i> ( <i>K<sub>o25</sub></i> )	Michaelis–Menten constant for Rubisco for O <sub>2</sub> (standardized to 25 °C)	kPa
<i>O</i>	Partial pressure of O <sub>2</sub>	Pa
<i>Q<sub>2</sub></i>	Photosynthetically active radiation absorbed by PSII	μmol m <sup>-2</sup> s <sup>-1</sup>
<i>R</i>	Universal gas constant (8.314 J K <sup>-1</sup> mol <sup>-1</sup> )	J K <sup>-1</sup> mol <sup>-1</sup>
<i>R<sub>d</sub></i> ( <i>R<sub>d25</sub></i> )	Mitochondrial respiration in the light (standardized to 25 °C)	μmol m <sup>-2</sup> s <sup>-1</sup>
$\Delta S$ ( $\Delta S_{gm}$ , $\Delta S_v$ , $\Delta S_j$ )	Entropy factor used in Arrhenius temperature function	J mol <sup>-1</sup> K <sup>-1</sup>
<i>T</i>	Leaf temperature	K
<i>T<sub>opt</sub></i>	Optimum temperature	K (°C)
<i>V<sub>cmx</sub></i> ( <i>V<sub>cmx25</sub></i> )	Maximum rate of Rubisco carboxylation (standardized to 25 °C)	μmol m <sup>-2</sup> s <sup>-1</sup>
<i>α</i>	Fraction of PSII activity in the bundle sheath	
<i>Γ*</i> ( <i>Γ*<sub>25</sub></i> )	Chloroplastic CO <sub>2</sub> photocompensation point (standardized to 25 °C)	Pa
<i>θ</i>	Empirical curvature factor	
HB parameters associated with hierarchical priors and hyperpriors		
<i>Y<sub>25</sub></i>	Plant-level mean of any parameter ( <i>Y</i> ) standardized to 25 °C	
<i>μY<sub>25</sub></i>	Species-level mean of any parameter ( <i>Y</i> ) standardized to 25 °C	
<i>μ*Y<sub>25</sub></i>	Population-level mean of any parameter ( <i>Y</i> ) standardized to 25 °C	
<i>τ</i>	Precision (1/variance) parameter describing observation and measurement error	
<i>τ<sub>Yplant</sub></i>	Precision (1/variance) parameter describing plant-to-plant variation within species	
<i>τ<sub>Yspp</sub></i>	Precision (1/variance) parameter describing species-to-species variability	

*et al.* model of C<sub>3</sub> photosynthesis (Farquhar *et al.* 1980). The dependence of potential electron transport rate on absorbed irradiance was specified according to Farquhar & Wong (1984). Triose phosphate limitation was not considered here because this process is expected to rarely limit photosynthesis and is not commonly included in models to estimate photosynthetic parameters (Wohlfahrt *et al.* 1999b; Medlyn *et al.* 2002; Dubois *et al.* 2007). Modifications for mesophyll conductance (*g<sub>m</sub>*) were included using quadratic equations as described by von Caemmerer & Evans (1991), von Caemmerer (2000) and Niinemets *et al.* (2009a). In addition, when values of *C<sub>i</sub>* and internal oxygen concentration (*O*) were converted from μmol mol<sup>-1</sup> to Pa, they were also corrected for pressure, because the pressure among measurement sites was different from standard pressure (range: 77.3–97.5 kPa). When both the *A–C<sub>i</sub>* and *A–Q* data sets were included, the Farquhar *et al.* model was still used to model the expected photosynthetic rate, and thus both data sets simultaneously informed parameters in the

photosynthetic model. See Table 2 for a list of model equations and parameters used to describe  $\bar{A}_i$  in Eqn 1.

Temperature dependencies of Rubisco's carboxylation and oxygenation rates affect photosynthesis (Bjorkman, Badger & Armond 1980), as do the temperature dependencies of *V<sub>cmx</sub>* and *J<sub>max</sub>* (von Caemmerer 2000). Thus, temperature dependencies for all parameters (i.e. *K<sub>c</sub>*, *K<sub>o</sub>*, *Γ\**, *g<sub>m</sub>*, *R<sub>d</sub>*, *V<sub>cmx</sub>* and *J<sub>max</sub>*; Table 1) were chosen to follow an Arrhenius function (von Caemmerer 2000; Leuning 2002; Medlyn *et al.* 2002; Kattge & Knorr 2007) standardized to 25 °C. The general form of the Arrhenius function for parameter *Y* (where *Y* = *K<sub>c</sub>*, *K<sub>o</sub>*, *Γ\**, *g<sub>m</sub>*, *R<sub>d</sub>*, *V<sub>cmx</sub>* or *J<sub>max</sub>*) is:

$$Y = f_i(Y_{25}, E_Y, Tobs_i) = Y_{25} \exp \left[ \frac{E_Y(Tobs_i - 298)}{(298 \cdot R \cdot Tobs_i)} \right] \quad (2)$$

where *Y<sub>25</sub>* is the parameter at 25 °C, *E<sub>Y</sub>* is the activation energy of *Y*, *Tobs* is the leaf temperature (K) measured by the Li-6400 and *R* is the universal gas constant

Eqn no.	Equation
2.1	$\bar{A}_i = A_{c_i}, \text{ if } Ciobs_i < C_{crit}$ $\bar{A}_i = A_{j_i}, \text{ if } Ciobs_i > C_{crit}$
2.2	$A_{c_i} = \frac{-b + \sqrt{b^2 - 4ac}}{2a}$ $a = -\frac{1}{g_{m_i}}$ $b = \frac{(V_{cmax_i} - R_{d_i})}{g_{m_i}} + Ciobs_i + K_{c_i} \left( \frac{1 + O_i}{K_{o_i}} \right)$ $c = R_{d_i} \left[ Ciobs_i + K_{c_i} \left( \frac{1 + O_i}{K_{o_i}} \right) \right] - V_{cmax_i} (Ciobs_i - \Gamma_i^*)$
2.3	$A_{j_i} = \frac{-b + \sqrt{b^2 - 4ac}}{2a}$ $a = -\frac{1}{g_{m_i}}$ $b = \frac{\frac{J_i}{4} - R_{d_i}}{g_{m_i}} + Ciobs_i + 2\Gamma_i^*$ $c = R_{d_i} (Ciobs_i + 2\Gamma_i^*) - \frac{J_i}{4} (Ciobs_i - \Gamma_i^*)$
2.4	$J_i = \frac{Q_{2i} + J_{max_i} - \sqrt{(Q_{2i} + J_{max_i})^2 - 4\theta Q_{2i} J_{max_i}}}{2\theta}$ <p>where <math>\theta = 0.7</math> (Evans 1989)</p>
2.5	$Q_{2i} = Qobs_i \cdot \alpha (1 - f) / 2,$ <p>where <math>\alpha = 0.85</math> (von Caemmerer 2000) and <math>f = 0.15</math> (Evans 1987)</p>

**Table 2.** List of equations used in the photosynthesis process model

All equations are from Farquhar *et al.* (1980), Farquhar & Wong (1984) and von Caemmerer (2000). See Table 1 for abbreviations, definitions and units.

(8.314 J mol<sup>-1</sup> K<sup>-1</sup>). To include plant-level variation in the  $g_m$ ,  $R_d$ ,  $V_{cmax}$  and  $J_{max}$  parameters at 25 °C (i.e. the  $Y_{25s}$ ), these parameters were allowed to vary by curve (or plant). To account for potential species-level differences in temperature dependencies, the activation energies associated with the  $g_m$ ,  $R_d$ ,  $V_{cmax}$  and  $J_{max}$  parameters ( $E_m$ ,  $E_r$ ,  $E_v$  and  $E_j$ , respectively) were allowed to vary by species, such that for observation  $i$ , plant  $p$  and species  $s$ :

$$\begin{aligned} g_{m_i} &= f_1(g_{m25p}, E_{ms(p)}, Tobs_i) \\ R_{d_i} &= f_1(R_{d25p}, E_{rs(p)}, Tobs_i) \\ V_{cmax_i} &= f_1(V_{cmax25p}, E_{vs(p)}, Tobs_i) \\ J_{max_i} &= f_1(J_{max25p}, E_{js(p)}, Tobs_i) \end{aligned} \quad (3)$$

The notation  $s(p)$  is read as 's of p', which represents the species identity associated with each plant (i.e. plant is 'nested' in species). Because the Rubisco kinetic properties at 25 °C ( $\Gamma_{25}^*$ ,  $K_{c25}$  and  $K_{o25}$ ) and their associated activation energies ( $E_g$ ,  $E_{kc}$ ,  $E_{ko}$ ) have only been shown to vary by species (von Caemmerer 2000) and are generally not well informed by A-C<sub>i</sub> or A-Q data, we assume that these parameters vary at the species level such that:

$$\begin{aligned} \Gamma_i^* &= f_1(\Gamma_{25s(p)}^*, E_{gs(p)}, Tobs_i) \\ K_{c_i} &= f_1(K_{c25s(p)}, E_{kcs(p)}, Tobs_i) \\ K_{o_i} &= f_1(K_{o25s(p)}, E_{kos(p)}, Tobs_i) \end{aligned} \quad (4)$$

While Eqns 2 and 3 were used for analyses of both data sets, it was also recognized that temperature response functions for  $g_m$ ,  $V_{cmax}$  and  $J_{max}$  are commonly modelled (von Caemmerer 2000; Leuning 2002; Medlyn *et al.* 2002; Kattge & Knorr 2007) using the peaked Arrhenius function (Johnson, Eyring & Williams 1942). As such, we also ran the model using the combined A-C<sub>i</sub> and A-Q data set with the peaked Arrhenius functions to determine if model fit and parameter estimation were improved by incorporating this more flexible temperature response compared to the non-peaked function in Eqn 2. For this analysis,  $f_1$  in Eqn 2 was replaced with:

$$\begin{aligned} Y &= f_2(Y_{25}, E_Y, Tobs_i, \Delta S_Y, H_Y) \\ &= Y_{25} \exp \left[ \frac{E_Y (Tobs_i - 298)}{298 \cdot R \cdot Tobs_i} \right] \frac{1 + \exp \left( \frac{298 \Delta S_Y - H_Y}{298 R} \right)}{1 + \exp \left( \frac{Tobs_i \Delta S_Y - H_Y}{R \cdot Tobs_i} \right)} \end{aligned} \quad (5)$$

where  $E_Y$  is the activation energy,  $H_Y$  is the deactivation energy describing the rate of decrease for temperatures above the optimum temperature and  $\Delta S_Y$  is an entropy factor. Once again,  $g_{m25}$ ,  $V_{cmax25}$  and  $J_{max25}$  parameters were allowed to vary by plant, and because species-level variation has been observed in the temperature response parameters (i.e.  $E$ ,  $H$ ,  $\Delta S$ ) (Kattge & Knorr 2007), the associated parameters for  $g_m$  ( $E_m$ ,  $\Delta S_{gm}$ ,  $H_{gm}$ ),  $V_{cmax}$  ( $E_v$ ,  $\Delta S_v$ ,  $H_v$ ) and  $J_{max}$  ( $E_j$ ,  $\Delta S_j$ ,  $H_j$ ) also were allowed to vary between species, such that:

$$g_{m_i} = f_2(g_{m25p}, E_{m_{s(p)}}, \Delta S_{m_{s(p)}}), H_{m_{s(p)}}, Tobs_i) \quad (6)$$

$$V_{cmax_i} = f_2(V_{cmax25p}, E_{v_{s(p)}}, \Delta S_{v_{s(p)}}), H_{v_{s(p)}}, Tobs_i)$$

$$J_{max_i} = f_2(J_{max25p}, E_{j_{s(p)}}, \Delta S_{j_{s(p)}}), H_{j_{s(p)}}, Tobs_i)$$

### The prior model

The final stage in the HB modelling approach was the specification of the priors for the unknown parameters. Because many model parameters varied on a plant and/or species level, nested, hierarchical priors were chosen. The ability to have nested priors is another major advantage of the HB approach because it allows parameters within a given level (e.g. across plants within species or across species) to inform or 'borrow strength' from each other (Carlin *et al.* 2006). Moreover, the nesting of plants within species within an overall population of desert shrubs describes a natural hierarchy that reflects the sampling design. Thus, under this framework, plant-level parameters – which are directly related to individual curve data – are assumed to be nested within species, such that for any plant-level parameter at 25 °C ( $Y_{25} = g_{m25}$ ,  $R_{d25}$ ,  $V_{cmax25}$  and  $J_{max25}$ ):

$$Y_{25p} \sim \text{Normal}(\mu Y_{25s(p)}, \tau_{Y_{plant}}) \quad (7)$$

where  $\mu Y_{25s(p)}$  is the species-level mean, and  $\tau_{Y_{plant}}$  is the precision (1/variance) parameter that describes plant-to-plant variability within a species. The species-level parameters were then assumed to be nested within an overall population, such that:

$$\mu Y_{25s} \sim \text{Normal}(\mu^* Y_{25}, \tau_{Y_{spp}}) \quad (8)$$

where  $\mu^* Y_{25}$  is the population-level mean, and  $\tau_{Y_{spp}}$  is the precision parameter that describes species-to-species variability within the desert shrubs studied here. Standard, independent and relatively non-informative (diffuse) priors were employed for the population-level mean parameters (the  $\mu^* Y_{25}$ ); that is, we used normal densities with large variances (small precisions). Folded-Cauchy (i.e. a Student's  $t$ -distribution with one degree of freedom) densities were assigned as priors for all standard deviations ( $\sigma = 1/\sqrt{\tau}$ , where  $\tau$  is the precision parameter of interest) as suggested by Gelman (2006). Another advantage of the HB framework is that we were able to incorporate informative priors for the Michaelis–Menten parameters ( $K_c$  and  $K_o$ ),

CO<sub>2</sub> compensation point ( $\Gamma^*$ ) and the Arrhenius temperature function parameters ( $E$ ,  $\Delta S$ ,  $H$ ); that is, we assigned normal distributions centred on values reported in the literature (von Caemmerer 2000) and used small precisions based on coefficients of variation (CV = standard deviation/mean) around 15% (Supporting Information Table S1).

Finally, another advantage of this HB approach is that we were able to specify which parameters should be informed by which data set. For example, we do not expect the  $A-Q$  data to contain sufficient information about  $V_{cmax}$  because the data were collected under ambient CO<sub>2</sub>, and  $C_i$  was approximately constant. Thus, within the HB model code (see WinBUGS implementation below), we employed the 'cut' function to sever the feedback between, for example, the  $A-Q$  curve data and  $V_{cmax}$ . This resulted in posterior distributions for parameters describing  $V_{cmax}$  that were solely informed by the  $A-C_i$  data, but the uncertainty in the  $V_{cmax}$  values was propagated to the predicted photosynthetic values associated with the  $A-Q$  data. Using this approach, we assumed that  $K_c$ ,  $K_o$ ,  $\Gamma^*$ ,  $g_m$ ,  $V_{cmax}$  and  $J_{max}$  were solely informed by the  $A-C_i$  data, and  $R_d$ ,  $C_{crit}$  and temperature dependence parameters were informed by both data sets (i.e. did not use the cut function with these parameters). Although  $A-C_i$  curve data generally do not provide sufficient data on  $R_d$  (i.e. all  $Aobs$  measurements were made under constant, high light), we still allow the  $A-C_i$  data to inform  $R_d$  because many studies may only measure  $A-C_i$  curves in an effort to estimate photosynthetic parameters, including  $R_d$ .

The HB model defined by Eqns 1–8 was implemented in the Bayesian statistical software package WinBUGS (Lunn *et al.* 2000). WinBUGS code for the HB model has been provided as supplementary material. Three parallel Markov chain Monte Carlo (MCMC) chains were run for 30 000 iterations each, and the BGR diagnostic tool was used to evaluate convergence of the chains to the posterior distribution (Brooks & Gelman 1998; Gelman 2004a). The burn-in samples (first 4000) were discarded, and the remaining samples (after convergence) were thinned every 20th iteration, yielding an independent sample of 3000 values for each parameter from the joint posterior distribution (Gelman 2004b; Gamerman & Hedibert 2006). Model goodness-of-fit was evaluated by using Eqn 1 to generate replicated data for the observed values ( $Aobs_i$ ) (Gelman *et al.* 2004), yielding posterior predictive distributions for each observation. If the model perfectly predicted the data, all observed-versus-predicted (posterior means for replicated data) points would lie exactly on the 1:1 line. We compared models (e.g.  $A-C_i$  data model with non-peaked temperature functions versus  $A-C_i$  data model with peaked temperature functions) by computing the posterior predictive loss ( $D$ ) for each model (Gelfand & Ghosh 1998).  $D$  is a model comparison statistic that accounts for model predictive ability ('goodness-of-fit') while penalizing for model complexity, and the model with the lower  $D$  value is preferred.

**Table 3.**  $r^2$  Values for observed versus predicted photosynthesis, posterior predictive loss ( $D$ ) and estimates of the uncertainty in the  $D$  values (i.e. approximate estimates of the 2.5th and 97.5th percentiles) obtained from the hierarchical Bayesian (HB) model using  $A-C_i$  data only and combined  $A-C_i$  and  $A-Q$  data with either non-peaked or peaked temperature response functions for photosynthetic parameters

Data/model combination	$r^2$	$D$	2.5%	97.5%
$A-C_i$ only (non-peaked temp.)	0.99	204.7	157.4	265.7
$A-C_i$ only (peaked temp.)	0.99	199.3	150.3	261.4
$A-C_i$ and $A-Q$ (non-peaked temp.)	0.76	31 960	22 820	41 250
$A-C_i$ and $A-Q$ (peaked temp.)	0.87	22 150	13 510	32 750

Note that comparison of the  $D$  values is only relevant within a given data set.

## RESULTS

### Model goodness-of-fit and model comparison

The coupled HB–photosynthetic model fit the data well for  $A-C_i$  data only and for the combined  $A-C_i$  and  $A-Q$  data using both non-peaked and peaked temperature functions (Table 3). For example, points in the plots of observed-versus-predicted photosynthesis fell tightly along the 1:1 line (data not shown). When comparing among models (for a particular data set or data set combination), models that incorporated peaked temperature responses had lower  $D$  values compared to models that used non-peaked temperature functions (Table 3). Thus, the results reported below, unless otherwise specified, are from models that employed peaked temperature functions for photosynthetic parameters of interest ( $g_m$ ,  $R_d$ ,  $V_{\text{cmax}}$  and  $J_{\text{max}}$ ).

### Utility of $A-Q$ data for estimates of biochemical parameters

While the model goodness-of-fit results were not statistically different for both  $A-C_i$  data only, and  $A-C_i$  and  $A-Q$  data combined (Table 3), the addition of  $A-Q$  data greatly improved estimation of  $R_{d25}$ . Using both data sets, there was a high frequency of positive posterior mean estimates of  $R_{d25}$ , while in the model that used only  $A-C_i$  data, the lower credible intervals and the posterior means for  $R_{d25}$  were often negative (Fig. 1). While we did not estimate  $R_{d25}$  using only  $A-Q$  data in this study, we expect that our model estimates for  $A-C_i$  and  $A-Q$  data combined would be similar to  $A-Q$  only estimates given that  $A-C_i$  data collected here were not able to directly inform  $R_{d25}$  because of measurement at high light. The inclusion of  $A-Q$  data did not improve estimates of  $V_{\text{cmax}25}$  or  $J_{\text{max}25}$ , but this is expected because the  $A-Q$  data were not allowed to inform these parameters. Importantly, the ability of  $A-Q$  data to inform biochemical parameters other than  $R_{d25}$  was limited by our  $A-Q$  measurements at ambient  $[\text{CO}_2]$ . By measuring  $A-Q$

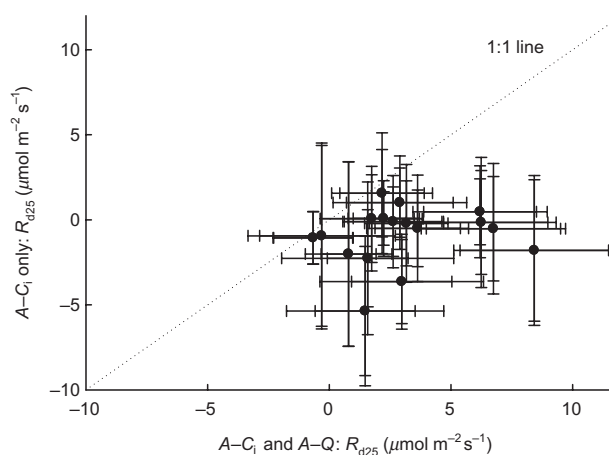
curves at above or saturating  $[\text{CO}_2]$ ,  $A-Q$  data could be used to inform additional biochemical parameters of interest (e.g.  $J_{\text{max}25}$ ). However, because both data sets did inform a subset of parameters, the inclusion of  $A-Q$  data had a slight impact on parameter uncertainty such that the posterior estimates for  $V_{\text{cmax}25}$  or  $J_{\text{max}25}$  varied more between plant/species and their credible intervals were smaller when using only  $A-C_i$  data (Fig. 2; Supporting Information Fig. S2). The use of  $A-Q$  data produced more variability in posterior mean estimates and slightly wider posterior credible intervals for  $C_{\text{crit}}$ , but the range of  $C_{\text{crit}}$  values was similar using either data set (Fig. 2; Supporting Information Fig. S2).

### Parameters poorly informed by photosynthetic data

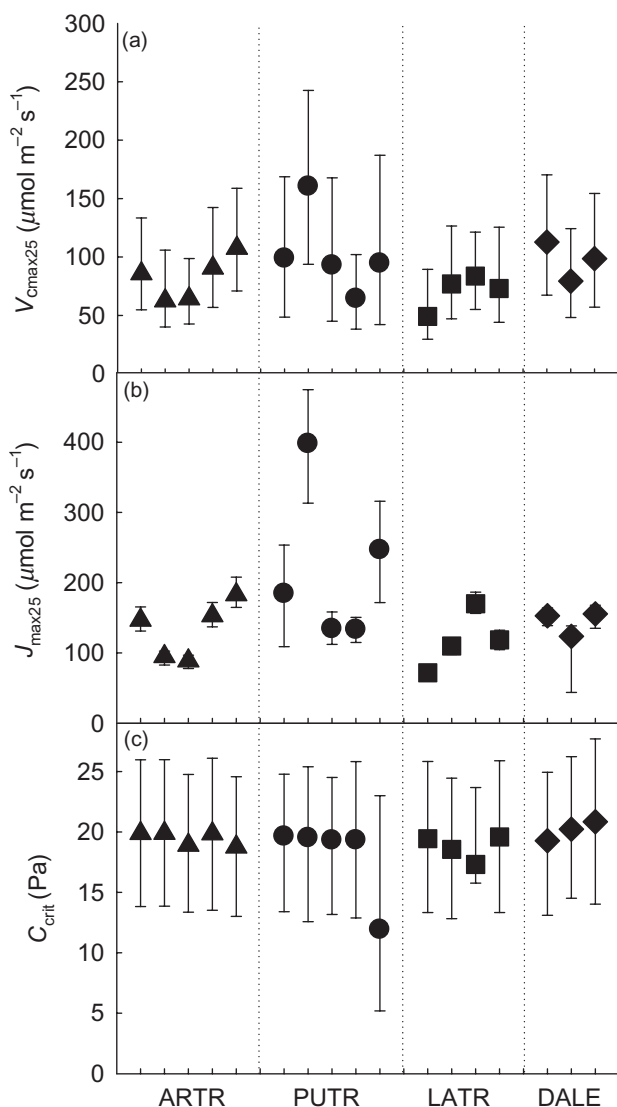
While the HB model provided an updated estimate of the Michaelis–Menten constant of Rubisco for  $\text{O}_2$  ( $K_{o25}$ ) that was informed by  $A-C_i$  data, this was not the case for all energy of activation parameters ( $E_{\text{kc}}$ ,  $E_{\text{ko}}$ ,  $E_{\text{gs}}$ ,  $E_{\text{m}}$ ,  $E_{\text{r}}$ ,  $E_{\text{v}}$ ,  $E_{\text{j}}$ ) and the peaked temperature parameters ( $H_{\text{gm}}$ ,  $H_{\text{v}}$ ,  $H_{\text{j}}$ ). That is, the posterior means for the species-level  $E$  and  $H$  parameters were very similar to the means specified by their informative prior distributions (Supporting Information Tables S1 & S2). This indicates that these parameters were poorly informed by the photosynthetic data used (Table 4), or the data are in close agreement with the priors. The first explanation is more likely because these parameters became less identifiable under less informative priors.

### Parameters well informed by photosynthetic data

The HB model produced posteriors for curve-specific  $C_{\text{crit}}$  values (used to differentiate between Rubisco- and



**Figure 1.** Posterior mean estimates and 95% credible intervals for the plant-level mitochondrial respiration rate standardized to 25 °C ( $R_{d25}$ ) from the peaked temperature model using only  $A-C_i$  data compared to estimates using both  $A-C_i$  and  $A-Q$  data.  $R_{d25}$  estimates from the combined data sets are greater than zero, while many of the  $R_{d25}$  estimates from the ‘ $A-C_i$  only’ data are negative.



**Figure 2.** Posterior mean estimates and 95% credible intervals for the plant-level values (i.e.  $Y_{25p}$  in Eqn 2) given by the hierarchical Bayesian (HB) model that incorporated  $A-C_i$  data only and that implemented the peaked temperature response functions. Estimates are shown for (a) maximum rate of carboxylation standardized to 25 °C ( $V_{cmax25}$ ), (b) maximum rate of electron transport standardized to 25 °C ( $J_{max25}$ ) and (c) plant-level transition intercellular partial pressure of  $CO_2$  ( $C_{crit}$ ). Plant-level estimates are grouped by species where ARTR = *Artemisia tridentata*, PUTR = *Purshia tridentata*, LATR = *Larrea tridentata* and DALE = *Dasyliirion leiophyllum*. Symbols correspond to species where ▲ = *A. tridentata*, ● = *P. tridentata*, ■ = *L. tridentata*, ◆ = *D. leiophyllum*. Plants are considered different if the posterior mean for one plant is not contained in the 95% CI for another plant.

RuBP-limited rates) that were well informed by the data, regardless of the data set used. These  $C_{crit}$  posterior means ranged from 11.9 to 22.1 Pa across all curves analysed (Fig. 2; Supporting Information Fig. S2). On a plant level, the HB model estimates of  $g_{m25}$ ,  $R_{d25}$ ,  $V_{cmax25}$  and  $J_{max25}$  were also well informed by the photosynthetic data (Figs 1–3).

This was demonstrated by narrow credible intervals, posterior means that were quite different from the corresponding prior means, and species differences for some of the parameters ( $R_{d25}$ ,  $J_{max25}$ ; Fig. 4). Moreover, many studies have observed a strong, linear correlation between  $V_{cmax25}$  and  $J_{max25}$  (i.e.  $J_{max25}$  tends to be two times  $V_{cmax25}$ ) (Wullschlegel 1993; Leuning 1997; Medlyn *et al.* 2002; Kattge & Knorr 2007). We did not impose any restrictions on the relationship between  $V_{cmax25}$  and  $J_{max25}$  in our HB model, and we used the model results to evaluate the relationship between these two parameters. The average ratio between the posterior means for plant-level  $J_{max25}$  and  $V_{cmax25}$  was estimated to be  $1.74 \pm 0.37$  across all species, and  $V_{cmax25}$  and  $J_{max25}$  were strongly correlated when using  $A-C_i$  data only (Fig. 5). This correlation, however, becomes weaker upon incorporation of the  $A-Q$  data.

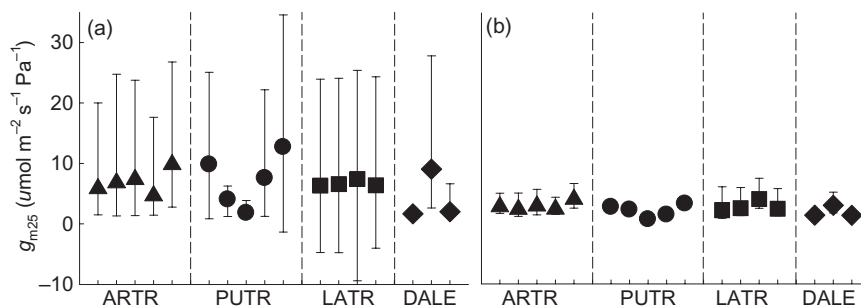
The potential for photosynthetic data to inform model parameters, which are not typically allowed to vary on a

**Table 4.** Classification of posterior estimates for parameters in the photosynthetic model obtained from the hierarchical Bayesian (HB) analysis using both  $A-C_i$  and  $A-Q$  data, and peaked temperature functions

Parameter	Well informed	Poorly informed	Species-level differences	Plant-level differences
$K_{c25}$	×		×	n/a
$K_{o25}$		×		n/a
$\Gamma^{*25}$	×*			n/a
$R_{d25}$	×		×	×
$V_{cmax25}$	×			×
$J_{max25}$	×		×	×
$E_{kc}$		×		n/a
$E_{ko}$		×		n/a
$E_g$		×		n/a
$E_m$		×		n/a
$E_r$		×		n/a
$E_v$		×		n/a
$E_j$		×		n/a
$g_m$	×			×
$\Delta S_{gm}$	×*			n/a
$H_{gm}$		×		n/a
$\Delta S_v$	×		×	n/a
$H_v$		×		n/a
$\Delta S_j$	×		×	n/a
$H_j$		×		n/a

Posterior means and credible intervals (CIs) were evaluated and compared to the prior means and CIs to determine the degree to which parameter estimates were informed by the photosynthetic data. Estimated parameters were classified as well informed by observed data if the posterior means were different from the prior means, had narrow CIs and/or exhibited plant- or species-level variation. Estimated parameters were poorly informed if the posterior estimates were similar to the prior means and had wide CIs. Parameter estimates were also evaluated to determine if they differed between species. An × in a cell indicates how a parameter was classified; an asterisk (\*) indicates the parameter was constrained by an informative prior distribution and may become well informed if the priors are relaxed. (For example, although the prior was informative, the posterior mean estimate was different from the prior mean on a plant or species level.)





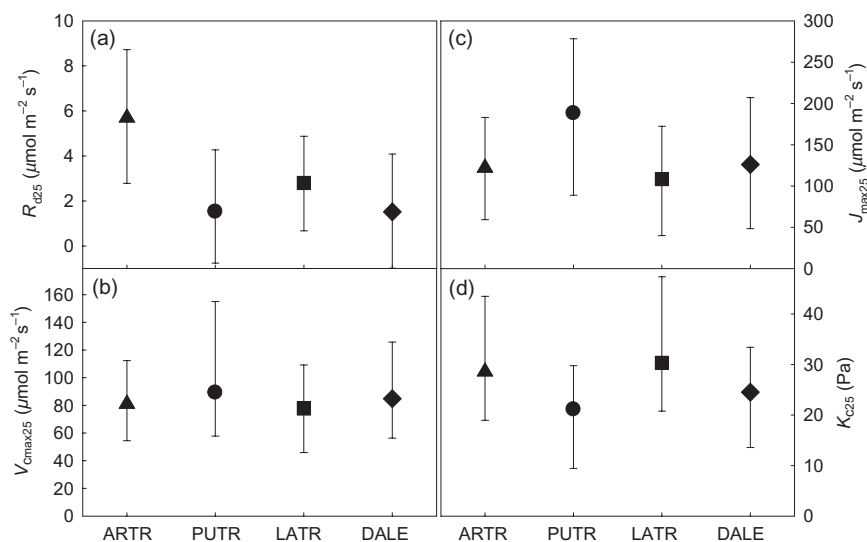
**Figure 3.** Posterior mean estimates and 95% credible intervals for the plant-level values for mesophyll conductance standardized to 25 °C ( $g_{m25}$ ) given by the hierarchical Bayesian (HB) model that incorporated  $A-C_i$  data only and that implemented the (a) peaked and (b) non-peaked temperature response functions for the four study species (see Fig. 2 for species abbreviations and symbol codes). Plants are considered different if the posterior mean for one plant is not contained in the 95% CI for another plant.

plant and species level, was demonstrated by significant species differences in posterior mean estimates ( $K_{c25}$ ,  $\Delta S_v$  and  $\Delta S_j$ ) and variability in the width of their credible intervals (Fig. 4; Supporting Information Fig. S3). Species-level estimates of  $\Gamma^*_{25}$  and  $\Delta S_{gm}$  were constrained by informative prior distributions, but may become well informed if the priors are relaxed. For example, species-level posterior mean estimates of  $\Gamma^*_{25}$  ranged from 4.7 to 5.9 Pa (Supporting Information Fig. S3), which is greater than the value currently used in most photosynthetic models (3.86 Pa, von Caemmerer *et al.* 1994). While the posterior credible intervals for the two species-level estimates of  $\Gamma^*_{25}$  did contain the prior mean value of 3.86 Pa, estimates for the other two species were significantly different, thus supporting the potential for this parameter to become well informed with

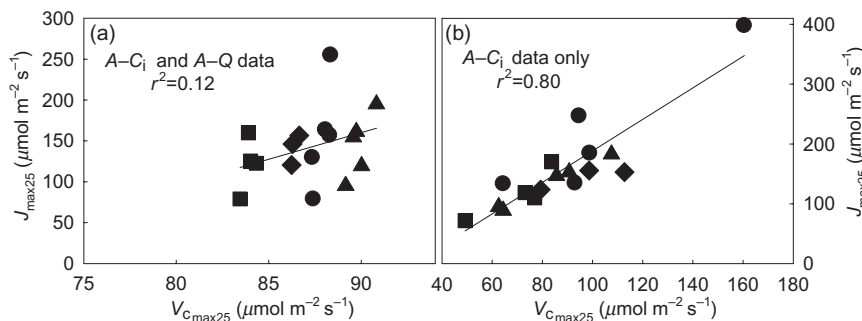
relaxed priors. Interestingly, plant-level model estimates of  $g_{m25}$  using the non-peaked temperature functions had narrower credible intervals than model estimates of  $g_{m25}$  using the peaked temperature functions (Fig. 3). All results are summarized in Table 4.

## DISCUSSION

We used an HB framework to couple the Farquhar *et al.* model with photosynthetic data to estimate plant- and/or species-level variability in kinetic constants, biochemical and photosynthetic parameters. The HB approach was successful in that it explicitly estimated the uncertainty or variability in the photosynthetic parameters, many of which are often held constant in applications of the Farquhar *et al.*



**Figure 4.** Posterior mean estimates and 95% credible intervals for the species-level values (i.e.  $\mu Y_{25s}$  in Eqn 8) given by the hierarchical Bayesian (HB) model that implemented the peaked temperature response function and that incorporated both  $A-C_i$  and  $A-Q$  data for (a) mitochondrial respiration standardized to 25 °C ( $R_{d25}$ ), and only  $A-C_i$  data for (b) maximum rate of carboxylation standardized to 25 °C ( $V_{cmax25}$ ), (c) maximum rate of electron transport standardized to 25 °C ( $J_{max25}$ ) and (d) Michaelis–Menten constant of ribulose 1-5-bisphosphate carboxylase/oxygenase (Rubisco) for  $CO_2$  standardized to 25 °C ( $K_{c25}$ ) for the four study species (see Fig. 2 for species abbreviations and symbol codes). Species are considered different if the posterior mean for one species is not contained in the 95% CI for another species.



**Figure 5.** The relationship between plant-level posterior mean estimates for  $V_{cmax25}$  (maximum rate of carboxylation) and  $J_{max25}$  (maximum rate of electron transport) standardized to 25 °C. That is, the points are the posterior means for plant-specific values of  $V_{cmax25}$  and  $J_{max25}$  based on the hierarchical Bayesian (HB) model that incorporated peaked Arrhenius temperature functions and used either (a)  $A-C_i$  data only or (b)  $A-C_i$  and  $A-Q$  data combined. Symbols correspond to species where  $\blacktriangle$  = *Artemisia tridentata*,  $\bullet$  = *Purshia tridentata*,  $\blacksquare$  = *Larrea tridentata*,  $\blacklozenge$  = *Dasyliirion leiophyllum*.

model. For example, variability in parameters associated with temperature dependence (e.g.  $E$ ) and Rubisco properties (e.g.  $K_{c25}$ ) was accounted for and estimated in the HB model (see Supporting Information Table S2), in addition to estimating parameters more directly linked with photosynthesis ( $g_m$ ,  $R_d$ ,  $V_{cmax}$ ,  $J_{max}$ ).

These parameters could be estimated via the rigorous HB statistical approach that accommodated multiple types of response curve data and that incorporated simultaneous plant-level estimates of  $C_{crit}$ .  $C_{crit}$  is a critical parameter in the model because it dictates the value of  $C_i$  used to differentiate between Rubisco and RuBP limitations. Usually,  $C_{crit}$  values are manually set at approximately 20–25 Pa based on work with *Phaenolus vulgaris* (von Caemmerer & Farquhar 1981; Wullschlegel 1993; Wohlfahrt *et al.* 1999b; Bunce 2000), but this relatively ad hoc approach to fitting the Farquhar *et al.* model to gas exchange data and the assumption of a fixed transition value across species has been contested (Ethier & Livingston 2004; Dubois *et al.* 2007). The need for a plant- and/or species-specific  $C_{crit}$  value has been supported by recent studies on trees (e.g. Douglas fir trees, Ethier & Livingston 2004), and was even demonstrated by early studies that transformed relationships between photosynthesis and chloroplastic  $CO_2$  ( $C_c$ ) into rates of RuBP regeneration or actual rates of electron transport, and then plotted these values against  $C_c$  to determine  $C_{crit}$  (von Caemmerer & Farquhar 1981; Kirschbaum & Farquhar 1984). The HB approach described herein provides a feasible method for estimating this key parameter.

In addition to our statistical fitting approach, this study is unique in its simultaneous use of both  $A-C_i$  and  $A-Q$  curve data to inform estimates of photosynthetic parameters. With the inclusion of  $A-Q$  data, estimates of  $R_{d25}$  were positive and therefore more biologically realistic. Other studies that fit the Farquhar *et al.* model to  $A-C_i$  data have had difficulty in obtaining accurate or biologically realistic estimates of  $R_{d25}$  (but see Dubois *et al.* 2007), and as such,  $R_{d25}$  is sometimes not reported (Medlyn *et al.* 2002). Additionally, when using the combined data set, species differences in  $R_{d25}$  were observed where *A. tridentata* had a significantly greater  $R_{d25}$

( $5.7 \mu\text{mol m}^{-2} \text{s}^{-1}$ ) than the other three species ( $1.5$ – $2.8 \mu\text{mol m}^{-2} \text{s}^{-1}$ ). Although knowledge about the regulation of  $R_d$  is generally limited (Nunes-Nesi, Sweetlove & Fernie 2007), recent work using isotopic techniques has shown that  $R_d$  plays a role in sustaining photorespiratory nitrogen cycling and perhaps nitrate assimilation (Tcherkez *et al.* 2008). This implies that *A. tridentata* may differ in nitrogen-use efficiency or ATP requirements for the sucrose synthesis and tricarboxylic acid (TCA) cycle intermediates compared to other desert species (Tcherkez *et al.* 2008). Furthermore, in some photosynthetic models,  $R_d$  is modelled as a function of  $V_{cmax}$ , where  $R_d$  set at 0.01–0.02 times  $V_{cmax}$  (von Caemmerer 2000); this relationship has been invoked to account for correlations between  $R_d$  and leaf nitrogen. At similar temperatures, the posterior means for  $R_{d25}$  were on average 0.03 times  $V_{cmax25}$  and were within the range of reported literature values from *in vivo* measurements (Bernacchi *et al.* 2001; Warren & Dreyer 2006). By assimilating both  $A-C_i$  and  $A-Q$  data, the HB approach estimated this ‘difficult’ parameter on both a species and plant level, and the estimates were consistent with values reported in the literature based on direct measurements of  $R_d$  (Bernacchi *et al.* 2001; Warren & Dreyer 2006).

The type of temperature response function needed to accurately fit the Farquhar *et al.* model to photosynthetic data is often species dependent (e.g. Medlyn *et al.* 2002). Subsequently, we compared model fit between the standard, exponential Arrhenius function (Eqn 2) and the peaked exponential function (Eqn 5), and model goodness-of-fit improved with the peaked function model. Some studies suggest that the peaked function is over-parameterized, thereby increasing the difficulty in estimating photosynthetic parameters (Harley *et al.* 1992; Dreyer *et al.* 2001; June, Evans & Farquhar 2004). Conversely, we found that the peaked function was best suited for our native desert plants, which are often exposed to hot and highly variable temperatures. However, it should be noted that posterior mean estimates of  $g_{m25}$  had tighter credible intervals and more plant-level variability using the non-peaked model compared to the peaked model. Poor estimates of  $g_m$  using the

peaked model may be caused by incorporating prior knowledge of  $g_m$  temperature dependencies based on plants from mesic ecosystems. While estimates of  $g_m$  for  $C_3$  herbaceous annuals and woody perennials in mesic ecosystems have been shown to be affected by environmental conditions such as soil water deficit (Flexas *et al.* 2002, 2009; Galle *et al.* 2009; Perez-Martin *et al.* 2009), few studies report how temperature affects  $g_m$  in desert species. Further study of the effect of environmental variation on  $g_m$  in desert plants is needed to correctly parameterize temperature dependency functions for these species.

Utilization of peaked temperature functions was further supported in that species differences were observed for estimates of the temperature function parameters  $\Delta S_v$  (with the inclusion of  $A-Q$  data) and  $\Delta S_j$  (using  $A-C_i$  data only; Supporting Information Fig. S3). Interestingly, both  $\Delta S_v$  and  $\Delta S_j$  were given informative prior distributions (Supporting Information Table S1), but the data resulted in posteriors that differed from the priors and that varied among species. To explore the implications of these differences for species-specific temperature responses, we recognize that the optimum temperature for  $V_{cmax}$  and  $J_{max}$  ( $T_{opt}$ ) is inversely proportional to  $\Delta S$  (Medlyn *et al.* 2002; Kattge & Knorr 2007). For example, *P. tridentata* in the Great Basin Desert had greater values for  $\Delta S_v$  (lower  $T_{optv}$ ) than plants in the Mojave Desert (*L. tridentata*) and Chihuahuan Desert (*D. leiophyllum*). *P. tridentata* had significantly greater values for  $\Delta S_j$  (lower  $T_{optj}$ ) than all other species. Further, these differences in  $T_{opt}$  may reflect differences in plant growth temperatures (Hikosaka, Murakami & Hirose 1999; Medlyn *et al.* 2002; Bernacchi, Pimentel & Long 2003; Onoda, Hikosaka & Hirose 2005). Because the Great Basin Desert is a cold desert, and the Mojave and Chihuahuan Deserts are hot deserts, the optimum temperature for maximum carbon assimilation in our study species may be related to growing season temperature. Indeed, in an analysis of 36 species, Kattge & Knorr (2007) found that plant growth temperature did not significantly affect  $V_{cmax}$  at a given base rate temperature, but did affect  $T_{opt}$  for  $V_{cmax}$ .

Species differences were also observed for model estimates of  $K_{c25}$  and  $J_{max25}$ . Because  $K_{c25}$  was assigned an informative prior distribution based on literature data that were the same for all species (Supporting Information Table S1), the photosynthetic curve data, and not the prior distribution, were the primary determinants of the posterior estimates of  $K_{c25}$ . Few modelling studies have estimated Michaelis-Menten parameters ( $K_{c25}$ ,  $K_{o25}$ ) because of the difficulty in collecting field data directly related to these parameters (but see von Caemmerer 2000; Ethier & Livingston 2004); interestingly, observed data influenced the posterior distributions for  $K_{c25}$  in this study. While this parameter describes intrinsic properties of Rubisco and is generally assumed constant across species (von Caemmerer 2000), our results show that  $K_{c25}$  should not be held constant across plants, species and functional types when estimating  $V_{cmax}$  and  $J_{max}$ . Importantly, we did not assume constant values for the kinetic constants or the temperature response parameters, but rather used informative priors to account

for variability, thereby obtaining more accurate estimates for parameters directly related to  $V_{cmax}$  and  $J_{max}$ .

Posterior estimates of species-level  $J_{max25}$  showed that it was significantly greater in *P. tridentata* compared to *A. tridentata* and *L. tridentata*. Given that  $J_{max25}$  may be influenced by environmental conditions (e.g. light, soil moisture), these results suggest that *P. tridentata* may have comparatively greater access to resources compared to the other species. This is partially supported by the observation that *P. tridentata* has a bimodal rooting distribution (Loik 2007), and thus it may utilize both stable (deep) and ephemeral (near-surface) water sources. Its surface roots may also facilitate uptake of nutrients from shallow soil layers. Greater access to water and nutrients is expected to increase the efficiency of electron transport. Because species have varying strategies for adapting to different environments, we suggest that photosynthesis should be measured under a wide range of environmental conditions (e.g. rooting depth, high-temperature stress, nutrient limitation, low soil moisture) and subsequently analysed using the flexible HB approach described herein. Using this approach, one can explicitly acknowledge important sources of uncertainty and accommodate variation in environmental drivers, existing knowledge about the photosynthetic process and parameters and diverse data sets to obtain more accurate estimates of species-level photosynthetic parameters (e.g.  $V_{cmax25}$ ,  $J_{max25}$ ).

In addition to accounting for species-level variability, results from our HB fitting approach highlight the importance of recognizing plant-level variability when estimating photosynthetic parameters using the Farquhar *et al.* model. Significant plant-level variation was observed for  $g_m$ ,  $R_d$ ,  $V_{cmax25}$  and  $J_{max25}$  (Figs 1–3). Because there was greater plant-level variation observed than species-level variation, this highlights the potential importance of small-scale variation in environmental variables for understanding photosynthetic responses in desert plants. Indeed, it has been well documented that  $V_{cmax25}$  exhibits high variation as a function of species identity, nutrient availability, season, leaf age and leaf position within the canopy (Medlyn *et al.* 1999; Wilson, Baldocchi & Hanson 2000; Misson *et al.* 2006). This study also indicates that plant-level variation must be accounted for when obtaining estimates of species-level photosynthetic parameters. Otherwise, if variability among plants is ignored, then the species-level parameter estimates and their associated uncertainties will be compromised.

## CONCLUSIONS

The HB approach presented herein allowed us to rigorously fit fairly complicated photosynthetic models to fairly simple data sets via a probabilistic modelling approach that: (1) simultaneously analysed diverse data sources (both  $A-C_i$  and  $A-Q$  curves) that informed the same underlying physiological processes; (2) explicitly accounted for and estimated parameter uncertainty for desert plant species, thereby filling a gap in our understanding of plant photosynthetic responses as most empirical studies have focused

on mesic temperate species; (3) avoided ad hoc model tuning by incorporating informative prior information derived from the literature to help constrain parameters that are not well informed by the field data (e.g. activation energies); and (4) did not require fixed parameter specifications, but rather was able to accommodate different degrees of model flexibility and prior information, allowing for a rigorous evaluation of photosynthetic parameters and different sources of variability. As such, the HB model of  $C_3$  photosynthesis successfully predicted observed photosynthesis. In addition, it yielded explicit plant-level estimates for  $C_{crit}$ , and plant- and species-level estimates for photosynthetic parameters ( $g_{m25}$ ,  $R_{d25}$ ,  $V_{cmax25}$  and  $J_{max25}$ ) for desert plants. In summary, the HB approach has great potential to improve the estimation of photosynthetic parameters across a wide range of  $C_3$  species, thereby extending the applicability and utility of process-based models such as the Farquhar *et al.* model. The ease of implementation and flexibility of the HB modelling approach make this an important tool that may be applied to a variety of ecosystems and experimental design settings.

## ACKNOWLEDGMENTS

We thank Travis Huxman, Michael Loik and Stan Smith for access to their study sites and use of their equipment. Assistance in the field and logistical support were provided by Holly Alpert, Greg Barron-Gafford, Topher Bentley, Jessie Cable, Dene Charlet, Dan Dawson, Earthwatch Mammoth Lakes SCAP students, Allison Ebbets, Alex Eilts, Lynn Fenstermaker, Alden Griffith, Danielle Ignace, Traesha Robertson, Joe Sirotiak, Anna Tyler and Natasja van Gestel. Victor Resco de Dios, Graham Farquhar and two anonymous reviewers provided valuable comments on earlier drafts of this manuscript. The research described in this paper has been funded in part by the United States Environmental Protection Agency (EPA) under the Greater Research Opportunities (GRO) Graduate Program (L.D.P.). EPA has not officially endorsed this publication, and the views expressed herein may not reflect the views of the EPA. This study was also supported by a US National Park Service grant (D.T.T.) and a US Department of Energy NICCR grant (K.O., D.T.T.).

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Received 5 June 2009; received in revised form 13 July 2009; accepted for publication 14 July 2009

## SUPPORTING INFORMATION

Additional Supporting Information may be found in the online version of this article:

**Figure S1.** Examples of typical gas exchange data collected from (a) a CO<sub>2</sub> response curve ( $A-C_i$ ) and (b) a light response curve ( $A-Q$ ).

**Figure S2.** Posterior mean estimates and 95% credible intervals for the plant-level values (i.e.  $Y_{25p}$  in Eqn 7) using the HB model with both  $A-C_i$  and  $A-Q$  data, and peaked temperature response functions for (a) maximum rate of carboxylation standardized to 25 °C ( $V_{cmax25}$ ), (b) maximum rate of electron transport standardized to 25 °C ( $J_{max25}$ ) and (c) plant-level transition intercellular partial pressure of CO<sub>2</sub> ( $C_{crit}$ ). Plant-level estimates are grouped by species where ARTR = *Artemisia tridentata*, PUTR = *Purshia tridentata*, LATR = *Larrea tridentata* and DALE = *Dasylium leiophyllum*. Symbols correspond to species where ▲ = *A. tridentata*, ● = *P. tridentata*, ■ = *L. tridentata*, ◆ = *D. leiophyllum*.

**Figure S3.** Posterior mean estimates and 95% credible intervals for the species-level values of the entropy factor used in Arrhenius temperature function ( $\Delta S$ ) for (a)  $g_{m25}$  (using  $A-C_i$  data only), (b)  $V_{cmax25}$  (using  $A-C_i$  and  $A-Q$  data), (c)  $J_{max25}$  (using  $A-C_i$  data only), as well as (d) the CO<sub>2</sub> compensation point in the absence of day respiration ( $\Gamma^{*25}$ ; using  $A-C_i$  data only) for the four study species using the hierarchical Bayesian (HB) model with peaked temperature functions (see Fig. S2 for species abbreviations and symbol codes).

**Table S1.** Median and 95% empirical quantiles for photosynthetic parameter values derived from the literature, with references provided; n/a indicates that information was not available in the literature. Refer to Table 1 for units.

**Table S2.** Posterior mean and 95% credible interval (CI) estimates for Michaelis–Menten parameters standardized to 25 °C ( $K_{c25}$ ,  $K_{o25}$ ), CO<sub>2</sub> compensation point in the absence of day respiration ( $\Gamma^{*25}$ ), activation energies ( $E_s$ ) and peaked Arrhenius temperature variables ( $H_s$ ,  $\Delta S_s$ ), given by the hierarchical Bayesian (HB) model for all four desert shrub species, using  $A-C_i$  data only. Posterior 95% CIs that do not contain the posterior mean of another species's parameter indicate significant differences between the two

parameter estimates; that is, there is at most a 5% chance that the species have similar parameter values. Refer to Table 1 for units.

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