

**Economics 520, Fall 2007**  
**Homework 3**  
**Due Tuesday, Sept 18 at beginning of class**

1. CB 2.7, part a.
2. CB 2.9
3. CB 2.14, part a.
4. CB 2.30, parts a, b.
5. The random variable  $X$  has a probability density function

$$f(x; \lambda) = \frac{\lambda^x \exp(-\lambda)}{x!}$$

for  $x = 0, 1, 2, \dots$  (i.e.  $X$  has a Poisson distribution with parameter  $\lambda$ ). In a lengthy manuscript, it is discovered that only 13.5 percent of the pages contain no typing errors. If we assume that the number of errors per page is a random variable with a Poisson distribution, find the percentage of pages with exactly one error.

6. Consider the following PDF:

$$f_X(x) = 3x^2, \quad 0 < x < 1.$$

- (a) Calculate (analytically)  $E(X)$  and  $V(X)$ .
- (b) Calculate (analytically) the median of  $X$ .
- (c) Using the `integrate` function in R, calculate the mean and variance of  $X$  and compare this to your result in part a. (Show any functions you define and commands used to calculate this.)
- (d) Using R, verify that the median calculated in part b is correct.